

# PAD: A Robustness Enhancement Ensemble Method via Promoting Attention Diversity

Yuting Yang\*, Pei Huang, Feifei Ma, Juan Cao and Jintao Li

Institute of Computing Technology, Chinese Academy of Sciences (CAS)

University of Chinese Academy of Sciences

Department of Computer Science, Stanford University

State Key Laboratory of Computer Science, Institute of Software, CAS

Laboratory of Parallel Software and Computational Science, Institute of Software, CAS

{yangyuting, caojuan, jtli}@ict.ac.cn, huangpei@stanford.edu, maff@ios.ac.cn

## Abstract

Deep neural networks can be vulnerable to adversarial attacks, even for the mainstream Transformer-based models. Although several robustness enhancement approaches have been proposed, they usually focus on some certain type of perturbation. As the types of attack can be various and unpredictable in practical scenarios, a general and strong defense method is urgently in require. We notice that most well-trained models can be weakly robust in the perturbation space, i.e., only a small ratio of adversarial examples exist. Inspired by the weak robust property, this paper presents a novel ensemble method for enhancing robustness. We propose a lightweight framework PAD to save computational resources in realizing an ensemble. Instead of training multiple models, a plugin module is designed to perturb the parameters of a base model which can achieve the effect of multiple models. Then, to diversify adversarial example distributions among different models, we promote each model to have different attention patterns via optimizing a diversity measure we defined. Experiments on various widely-used datasets and target models show that PAD can consistently improve the defense ability against many types of adversarial attacks while maintaining accuracy on clean data. Besides, PAD also presents good interpretability via visualizing diverse attention patterns.

**Keywords:** adversarial robustness, pre-trained language models, attention

## 1. Introduction

Deep neural networks (DNNs) have been broadly applied in various natural language processing (NLP) tasks. However, they are vulnerable to adversarial examples that are intentionally crafted by attackers for misleading the predictions of models with few perturbations, ranging from character-level, word-level to sentence-level. Character-level attacks (Li et al., 2019; Gao et al., 2018; Pruthi et al., 2019) usually insert, replace or delete some characters in the inputs. Most word-level attacks (Jin et al., 2020; Zang et al., 2020; Ren et al., 2019a) search adversarial examples in the synonym spaces with different search algorithms. Recently, pre-trained language models (PLMs) are also utilized to generate candidate substitutions (Yang et al., 2022a; Li et al., 2020). Sentence-level attacks manipulate new paraphrases for sentences, e.g., Iyyer et al. (2018) transform sentences with the desired syntax. With the emergence of more and more adversarial attacks, general and efficient methods for defending against adversarial attacks and enhancing robustness are of critical importance for developing trustworthy AI systems.

As a countermeasure, a series of defense methods are proposed targeted at certain specific attacks. Character-level perturbations can be cor-

rected via predicting the original words using context semantics (Pruthi et al., 2019). For word substitution-based attacks, Zhou et al. (2019) train a perturbation discriminator to identify malicious perturbations. Recently, few work begins to explore the feasibility of general defense methods. Although adversarial training (Wang et al., 2021; Liu et al., 2020; Alzantot et al., 2018) is a general defense method, it relies on the knowledge about target attacks and is time-consuming owing to the process of generating enough adversarial examples. Considering that many attacks rely on iterative search mechanisms, Le et al. (2022) proposes to confuse the attackers by automatically weighted ensembles of several classification layers. However, the frozen feature extraction module limits the diversity of models and the randomness of the ensemble brings instability to the outputs.

For well-trained DNNs, adversarial examples occupy a small ratio in most perturbation spaces (Yang et al., 2022b). In this case, the ensemble method can have a large probability of defending attack if the adversarial examples of different sub-models distribute in different regions. As the left part of Fig. 1 shows, the majority of sub-models make correct predictions for the input  $x$ , then the vote result of ensemble is also correct. Inspired by this, we want to develop an ensemble method to enhance robustness for Transformer-based models, which are the most popular architectures recently

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\*Corresponding author.

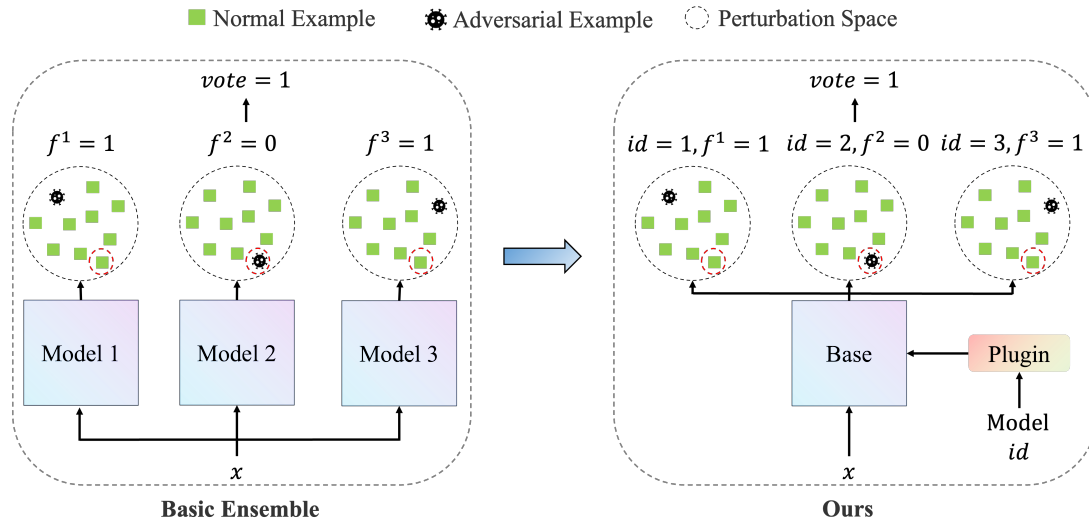


Figure 1: Illustration of ensemble method. The ensemble method can enhance robustness via diversifying the adversarial example distribution in the perturbation spaces. A lightweight plugin is designed to perturb the parameters of the base model.

due to their outstanding performances. Utilizing ensemble method to enhance robustness faces two main challenges: (1) How to train several sub-models with low computational resources, especially for large PLM-based models? (2) How to diversify the adversarial example distributions for different sub-models?

In order to diversify adversarial example distributions with as low computational resources as possible, we propose a novel ensemble method based on **promoting attention diversity** (PAD). To tackle the computational challenge, we design a lightweight plugin to learn the perturbation of parameters since sub-models generally share the same architectures but differ in the values of parameters as the right part of Fig. 1 shows. Instead of perturbing all parameters, PAD only perturbs some parameters of the first self-attention layer as attention module is one of the most important parts for feature extraction in Transformer-based models. Perturbing first-layer attention also provides good interpretability as they correspond to the attention on original input tokens.

Although different sub-models can be perturbed with different parameters at first, their parameters tend to be very similar while achieving coverage state as they share the same architectures and optimization goals. Intuitively, a true prediction can be made based on different attention patterns. Take a text (“I like this movie, it is really nice!”) in sentiment classification task as an example. If a model pays more attention to (“like”, “movie”) and the other two models pay more attention to (“movie”, “nice”), all of them can output positive classification results. Thus, the perturbation on “like” will be alleviated in the ensemble. To diversify the attention of different

models, we first define a measure for attention diversity based on the differences in attention score vectors and then optimize it in the training process.

We evaluate our method on experiments of three NLP tasks and two target models (BERT (Devlin et al., 2019) and RoBERTa (Liu et al., 2019)). Experimental results show that PAD significantly improves the robustness under different levels of attacks with an average increase of 9.2% robustness accuracy over the state-of-the-art defense baselines. Besides, PAD can maintain the performance on normal examples well. Via visualizing attention scores in different sub-models, our work also presents good interpretability which explains how the different sub-models make complementary decisions.

## 2. Preliminary

Given a natural language classifier  $f : \mathcal{X} \rightarrow \mathcal{Y}$ , which is a mapping function from an input space to an output label space. The input space  $\mathcal{X}$  contains all possible texts  $x$  and output space  $\mathcal{Y} = \{y_1, y_2, \dots, y_c\}$  contains  $c$  possible predictions of an input.

**(Adversarial Example)** Consider a classifier  $f(x)$ . Given a sequence  $x$  with gold label  $y^*$  and  $x'$  is a text generated by perturbing  $x$  with semantic preservation,  $x'$  is an adversarial example if:

$$f(x') \neq y^*. \quad (1)$$

**(Perturbation Space)** A perturbation space  $\Omega(x)$  of an input sequence  $x$  is a set containing all perturbations  $x'$  generated by perturbing the original input with semantic preservation.

**(Weak Robustness)** If the value of  $\mathbb{PR} > 1/2$ ,  $f$  is said to be weak robust on the perturbation space  $\Omega(x)$ , where  $\mathbb{PR}$  is the robustness metric:

$$\mathbb{PR} := \frac{|\{x' : x' \in \Omega(x) \wedge f(x') = y^*\}|}{|\Omega(x)|}. \quad (2)$$

$(1 - \mathbb{PR})$  measures the proportion of adversarial examples in the perturbation space, i.e., the probability of being altered by a random perturbation. Existing work observes that most well-trained NLP neural models satisfy weak robustness, e.g., BERT trained on IMDB dataset achieves  $\mathbb{PR}$  larger than 0.9 in 90.66% word substitution spaces (Yang et al., 2022b). As perturbation space  $\Omega(x)$  is difficult to be formally defined for other types of perturbations, we can not analyze the value of  $\mathbb{PR}$ . In this paper, we assume that well-trained DNNs can satisfy weak robustness for other types of perturbation, which is the prerequisite of our method.

### 3. Methodology

Ensemble learning is a generic approach to aggregating weak models into strong models and is usually effective to improve generalization performance. In this paper, we extend it to enhance weak robustness. Assuming that we have  $M$  well-trained deep models  $\{f^1, \dots, f^M\}$ , they are weakly robust on the perturbation space and their adversarial example distributions are different. A basic idea for reducing the number of adversarial examples is aggregating the predictions of individual  $M$  models, e.g., plurality voting. The prediction result  $\tilde{y}$  of the ensemble is:

$$\tilde{y} := \arg \max_{y \in \mathcal{Y}} \sum_{m \in [M]} \mathbb{I}(f^m(x) = y), \quad (3)$$

where  $f^m$  is  $m$ -th sub-model in the ensemble.

There still exists two issues that need to be addressed:

- 1 Modern popular Transformer-based models like BERT and RoBERTa are big with millions of parameters. Training several models can be very expensive which sometimes will be infeasible in terms of memory and time complexity.
- 2 Using the same training data and similar gradient-based training algorithms to train models with the same structure will result in homogeneous models. How to make the distribution of adversarial samples in the perturbation space of  $M$  models diverse?

To reduce computational resources, we propose to perturb the weights of the original network with an additional module, which is more like a plugin for a model. The models perturbed under different

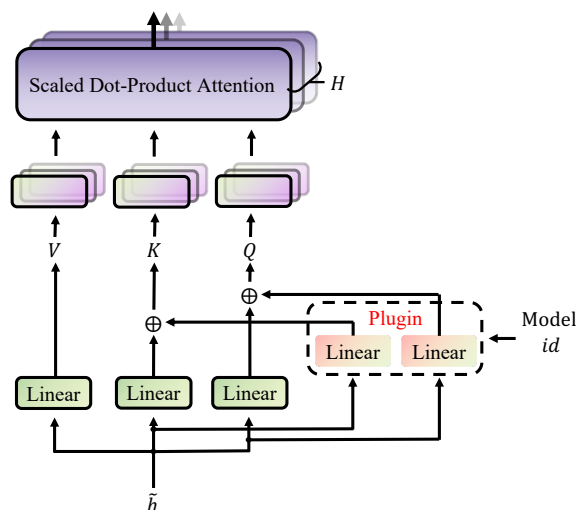


Figure 2: Diagram of the attention plugin module.

perturbations generated by the plugin can be seen as different models. To promote model diversity, we propose attention diversity which encourages different models to focus on different parts of an input sequence to make predictions.

#### 3.1. Plugin Module

In this section, we introduce how to construct the ensemble with a lightweight plugin module. Notice that if  $M$  models  $\{f^1, \dots, f^M\}$  in an ensemble have the same structure, then the main difference among these  $M$  members is their weights. So we can use small neural networks to generate perturbations for weights and produce different models. Formally, if  $f$  is a well-trained base model and  $\theta$  is its parameters, then we can produce  $f^m$  via modifying parameters  $\theta$  of  $f$  as

$$\theta^m = \theta + \Delta^m, \quad (4)$$

where  $\Delta^m$  can be generated by a small network.

In pursuit of efficiency and good interpretability, instead of perturbing all the parameters in the base model  $f$ , we only perturb some parameters of the first self-attention layer, since the attention module is one of the most important parts for feature extraction in modern NLP models. Besides, the first attention layer is close to the original input sequence and the attention score can be directly interpreted as the attention to the input sequence, which can provide better interpretability.

The query matrix  $Q$  and key matrix  $K$  of a self-attention module are usually transformed from a matrix  $\tilde{h}$  (hidden state or embedding) with linear layers.

$$Q = \text{Linear}_Q(\tilde{h}) = W_Q \tilde{h} + b_Q, \quad (5)$$

$$K = \text{Linear}_K(\tilde{h}) = W_K \tilde{h} + b_K. \quad (6)$$

We can generate  $f^m$  via perturbing parameters  $W_Q$ ,  $b_Q$ ,  $W_K$  and  $b_K$ . The query matrix  $Q_m$  and key matrix  $K_m$  of  $m$ -th member  $f^m$  can be obtained under perturbation  $\Delta^m$ :

$$\begin{aligned} Q^m &= (W_Q + \Delta_W^m)\tilde{h} + (b_Q + \Delta_b^m), \\ &= (W_Q\tilde{h} + b_Q) + (\Delta_W^m\tilde{h} + \Delta_b^m), \quad (7) \\ &= \text{Linear}_Q(\tilde{h}) + \text{Linear}_Q^m(\tilde{h}). \end{aligned}$$

Similarly, we have:

$$K^m = \text{Linear}_K(\tilde{h}) + \text{Linear}_K^m(\tilde{h}). \quad (8)$$

Thus, the parameters perturbation  $\Delta^m$  for  $f^m$  can be realized with additional linear layers  $\text{Linear}_Q^m(h)$  and  $\text{Linear}_K^m(h)$ . Fig. 2 is a diagram. For an input sequence  $x$ , it will be copied in  $M$  copies and concatenated with an index ( $id$ ) indicating which model to feed into. For example, an input  $\langle x, m \rangle$  indicates that the plugin will generate perturbations  $\Delta^m$  and constructs  $f^m$  to deal with the sequence  $x$ .

Suppose  $\mathcal{L}_{CE}^m$  is the classification loss of  $m$ -th member (e.g., cross-entropy loss), then one of the optimization objectives of the ensemble can be defined as:

$$\mathcal{L}_{CE} = \frac{1}{M} \sum_{m \in [M]} \mathcal{L}_{CE}^m. \quad (9)$$

### 3.2. Attention Diversity

If we only use  $\mathcal{L}_{CE}$  to train the ensemble, the parameters of different sub-models will tend to be very similar as they share the same architecture and optimization goal. In this section, we define a new loss to encourage the diversities among sub-models.

The self-attention mechanism allows the inputs to interact with each other (“self”) and find out to who they should pay more attention (“attention”). Sometimes the same prediction result can be given based on different attention patterns. For example, for a sentence “*I like this movie, it is really nice!*”, if a model pay more attention to (“like”, “movie”) and the other one pay more attention to (“movie”, “nice”), They both output positive sentiment classification results. Another case is that if both models have the highest attention on (“like”, “movie”) but with different values, they can also output the same classification result. Thus, promoting attention diversity can not only maintain accuracy but also improve the diversity of different sub-models. Further, it can affect the distributions of adversarial examples for each model.

Suppose  $A^m \in R^{H \times L \times L}$  represent the attention scores outputted by a self-attention layer of  $m$ -th model.  $H$  is the number of attention heads and  $L$

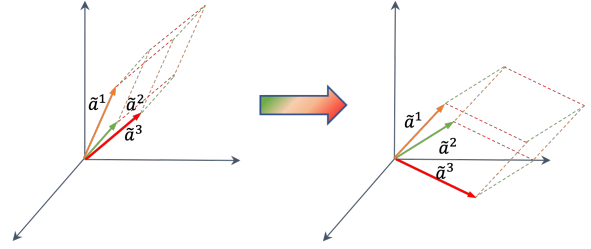


Figure 3: Diagram of promoting attention diversity.

is the sequence length. Then the sum score of all heads can be denoted as  $\hat{A}^m \in R^{L \times L}$ :

$$\hat{A}^m = \sum_{h \in [H]} A_h^m, \quad (10)$$

which can be regarded as the attention scores between any two token pairs.  $\hat{A}^m = (\hat{a}_1^m, \dots, \hat{a}_L^m)^\top$  with each row  $\hat{a}_l^m$  is the attention scores for  $l$ -th token position. We use  $\tilde{A}^m = (\tilde{a}_1^m, \dots, \tilde{a}_L^m)^\top$  to denote the matrix that each row  $\tilde{a}_l^m$  is obtained by normalizing  $\hat{a}_l^m$  in  $\hat{A}^m$  under  $\ell_2$ -norm, i.e.,  $\|\tilde{a}_l^m\|_2 = 1$ .

Let  $D_l$  ( $l \in [L]$ ) be the gather of the normalized attention scores of  $l$ -th token position for  $M$  models. It is denoted as:

$$D_l = (\tilde{a}_l^1, \dots, \tilde{a}_l^M)^\top. \quad (11)$$

Based on the matrix theory (Bernstein, 2009), the determinant of matrix computes the volume spanned by the vectors. Then we use the determinant of matrix  $D_l D_l^\top$  to measure the diversity among these attention vectors.

$$\det(D_l D_l^\top) = \text{Vol}^2(\tilde{a}_l^1, \dots, \tilde{a}_l^M), \quad (12)$$

where  $\text{Vol}(\cdot)$  is the volume of the geometry formed by vectors  $(\tilde{a}_l^1, \dots, \tilde{a}_l^M)$ . Intuitively, higher values of  $\det(D_l D_l^\top)$  indicate higher attention diversity as shown in Fig. 3.

In pursuit of diversities among models, we can minimize the attention diversity loss:

$$\mathcal{L}_{PAD} = -\frac{1}{L} \sum_{l \in [L]} \det(D_l D_l^\top). \quad (13)$$

To maintain accuracy and promote attention diversity, the minimization goal in the training process can be denoted as:

$$\mathcal{L} = \mathcal{L}_{CE} + \lambda \mathcal{L}_{PAD}, \quad (14)$$

where  $\lambda$  is a hyper-parameter for regulating the effect of the impact of attention diversity. While training, the original parameters of base models are frozen.



Dataset	Method	Character					Word				Sentence	
		VIPER			DeepWordBug		TextFooler		BertAttack		SCPN	
		Acc	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob
MR	Base	89.97	38.56	52.50	32.24	61.80	63.82	33.00	71.05	26.40	37.49	53.10
	ADV	89.78	39.68	51.00	34.95	59.20	53.19	42.60	65.05	31.80	39.90	51.00
	ASCC	89.87	38.16	53.00	21.88	71.40	<b>21.01</b>	72.20	56.67	39.60	37.09	53.60
	DNE	88.66	38.13	52.50	29.13	65.20	41.30	54.00	68.15	28.60	37.43	53.00
	SHIELD	89.97	36.25	53.50	18.08	75.20	29.54	64.40	54.92	40.20	37.45	53.20
	PAD	<b>89.97</b>	<b>35.42</b>	<b>55.50</b>	<b>9.73</b>	<b>83.50</b>	21.62	<b>72.50</b>	<b>21.93</b>	<b>73.00</b>	<b>36.19</b>	<b>57.50</b>
IMDB	Base	88.81	26.48	66.00	35.16	59.00	86.81	12.00	90.11	9.00	60.44	36.00
	ADV	88.70	<b>22.22</b>	69.00	16.57	73.00	56.57	38.00	74.44	23.00	63.33	32.00
	ASCC	87.72	28.53	64.50	15.82	81.50	48.96	53.50	79.01	18.00	69.77	26.00
	DNE	86.84	28.89	63.00	16.49	81.00	55.67	43.00	84.54	15.00	68.16	26.00
	SHIELD	88.81	24.61	66.00	17.14	72.50	36.00	56.00	69.66	27.00	59.14	36.50
	PAD	<b>88.81</b>	23.19	<b>69.00</b>	<b>8.79</b>	<b>83.00</b>	<b>30.77</b>	<b>63.00</b>	<b>37.36</b>	<b>57.00</b>	<b>58.64</b>	<b>38.00</b>
SNLI	Base	88.36	38.16	51.20	45.52	47.40	65.52	30.00	78.16	19.00	19.89	68.40
	ADV	85.03	39.55	50.20	43.93	49.60	53.28	33.10	77.45	20.30	23.08	61.40
	ASCC	82.98	38.50	47.20	31.52	57.80	56.75	34.60	75.25	19.80	21.75	60.60
	DNE	87.55	40.00	51.60	41.15	51.20	55.40	38.80	77.24	19.80	19.89	67.40
	SHIELD	88.34	37.25	52.30	40.78	51.40	53.46	40.40	71.43	24.80	19.49	68.20
	PAD	<b>88.36</b>	<b>36.05</b>	<b>53.60</b>	<b>8.51</b>	<b>79.60</b>	<b>37.47</b>	<b>54.40</b>	<b>51.03</b>	<b>42.60</b>	<b>17.13</b>	<b>69.80</b>

Table 1: Robustness evaluation results (%) of BERT-based target models. Only for Suc, the lower the value, the better the defense capability of the model. It is noted with ↓. The numbers in bold denote the best performance for the metric.

## 4. Experimental Setup

### 4.1. Datasets and Models

We conduct experiments on two important NLP tasks: text classification and natural language inference. For text classification, MR (Pang and Lee, 2005) and IMDB (Maas et al., 2011) are sentence-level and document-level classification tasks with two classes (positive and negative) respectively. SNLI (Bowman et al., 2015) is the dataset for the natural language inference task: whether the second sentence (hypothesis) can be derived from the first sentence (premise) with entailment, contradiction, or neutral relationship.

Target models include two popular deep neural architectures based on BERT (Devlin et al., 2019) and RoBERTa (Liu et al., 2019). BERT and RoBERTa are both the base versions with 12 layers, 768 hidden units, 12 heads, and 110M parameters.

### 4.2. Attacking Methods

We choose five adversarial methods for different levels of attacks. VIPER (Eger et al., 2019) modifies characters with visual-similar ones, e.g., replacing “wiki” with “w!k!”. DeepWordBug (Gao et al., 2018) performs small character-level perturbation targeting the important tokens in inputs. For word-level perturbation, TextFooler (Jin et al., 2020) is a greedy algorithm based on the word importance which is measured as the prediction change before and after deleting the word in a sentence. BertAttack (Li et al., 2020) uses the masked language

model (BERT) as a perturbation generator and finds perturbations that maximize the risk of making wrong predictions, which extends the perturbation space beyond synonyms. For sentence-level perturbation, we utilize SCPN (Iyyer et al., 2018) which transforms sentences with the desired syntax. All attack algorithms are implemented in the open framework *OpenAttack* (Zeng et al., 2021)<sup>1</sup>. To keep the semantics consistent after attacking, we limit the ratio of perturbation to be less than 0.25 and the similarity of sentence embedding to be larger than 0.5.

### 4.3. Defense Baselines

Four strong baselines for robustness enhancement are selected: ADV (adversarial training) (Wang et al., 2021; Ren et al., 2019b) usually retrains the model with adversarial examples. ASCC (Dong et al., 2021) models the word substitution space as a convex hull and optimizes adversaries generated in the hull. DNE (Zhou et al., 2021) expands convex hulls to two-hop synonyms neighbors and performs prediction via weighted average of the softmax probability vectors of all the randomly sampled sentences in the convex hull. SHILED (Le et al., 2022) is a general defense method which modifies the classification layer of a trained NN and conducts a stochastic weighted ensemble of different prediction heads.

<sup>1</sup><https://github.com/thunlp/OpenAttack>

## 4.4. Metrics and Settings

Three metrics are used for evaluating enhancement methods: clean accuracy (**Acc**), successful rate (**Suc**) and robustness accuracy (**Rob**). Acc is the the prediction accuracy of the original test data. Suc is the attack success rate. Rob measures the accuracy of a model under attack, which is the ratio of inputs that are correctly classified and not successfully attacked.

The weight of attention diversity  $\lambda$  in Eq. 3.2 is set to 0.1 which can make two losses on the same magnitude and make ensemble perform the best results. The number of sub-models is set to 3. PAD has only 1.08% parameters compared with training 3 models for ensemble.<sup>2</sup>

## 5. Experimental Results

### 5.1. Robustness Enhancement

We evaluate the performances of different enhancement methods on 500 data randomly sampled from test set and the experimental results are presented in Table 1 and 2 for BERT-based and RoBERTa-based models respectively. As generating adversarial examples is time-consuming, we only generate adversarial examples for 25% randomly sampled training data. Besides, a large number of adversarial examples will shift the original data distribution. ADV in Table 1 and 2 is conducted with word-level adversarial examples as a reference.

Compared with all enhancement baselines, PAD achieves the highest robustness (Rob) for all adversarial attacks and target models. The improvements are significant on DeepWordBug, TextFooler and BertAttack (more than 6% in Rob over the state-of-the-art baselines). As sub-models of PAD pay different attention to input tokens, some perturbation on tokens can be ignored in the ensemble. For the character-level DeepWordBug, e.g., replace “movie” with “moive”, the embedding vector is split and paid attention to by different heads. Thus, such perturbation is hard to deceive all attention patterns of the sub-models.

PAD achieves relatively moderate improvements on the two hard cases (VIPER and SCPN). Since VIPER modifies original characters with visually-similar ones, e.g., replace “1” with “l”, it sometimes generates examples out of the original data distribution. SCPN is relatively hard to be defended as it changes the structures of input sentences largely. Thus, sub-models can not learn them from the original data distribution and the ensemble will be ineffective.

<sup>2</sup>Code is available at <https://github.com/YANG-Yuting/PAD>

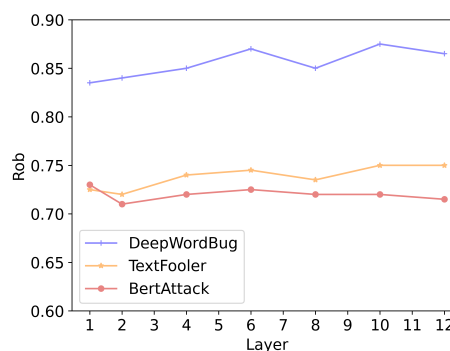


Figure 4: The robustness while performing perturbation on different attention layers of MR-BERT.

Compared with the defense methods designed for some target attacks, PAD performs consistent improvements under all types of attacks. ASCC and DNE aim at defending word-substitution perturbation and sometimes even decrease defense ability for other types of attacks, e.g., ASCC decreases 10% Rob of IMDB-BERT under the sentence-level attack SCPN. PAD also performs a good trade-off between clean accuracy and robustness, which always keeps the same Acc as the base model. Most existing methods improve robustness with the loss of accuracy including ADV, ASCC and DNE (even 5.38% decrease for ASCC on SNLI-BERT). Compared with the general defense method SHIELD, PAD diversifies the feature extraction process while SHIELD freezes it. Some adversarial examples can be caused by the feature extraction module which maps them to inappropriate embedding spaces. So PAD achieves better performance than SHIELD. The good performances of PAD indicate that the general robustness enhancement method is promising, especially under the trend of utilizing unified Transformer-based architectures in NLP domain.

Further, we compare PAD with ADV which re-trains the base model with different levels of adversarial examples. Experiment results on MR-BERT are presented in Table 3.  $ADV_c$ ,  $ADV_w$  and  $ADV_s$  means retraining the base model with character-level, word-level and sentence-level adversarial examples respectively.  $ADV_a$  utilizes these three levels of adversarial examples. ADV with adversarial examples of target attack can enhance the robustness against the attack, but becomes ineffective while encountering some other levels of attacks and even decreases the robustness ( $ADV_w$  decreases 1.5% Rob under VIPER, VP, compared with the base model).  $ADV_a$  stimulates the situation that simultaneously uses methods that resist different types of attacks. We find that  $ADV_a$  can improve robustness for all levels of attacks compared with the base model. However, the improvement is lower

Dataset	Method	Character					Word				Sentence	
		VIPER			DeepWordBug		TextFooler		BertAttack		SCPN	
		Acc	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob	Suc↓	Rob
MR	Base	90.07	22.78	67.50	32.17	62.00	65.65	31.40	66.67	30.00	31.67	59.50
	ADV	89.03	27.48	62.60	30.73	62.50	49.71	44.00	48.36	47.80	32.47	58.30
	ASCC	90.01	25.00	65.50	29.44	63.50	30.56	62.50	33.33	60.00	31.11	60.00
	DNE	90.03	27.16	63.73	28.11	65.00	29.83	61.50	30.15	57.01	31.60	59.50
	SHIELD	90.07	21.74	68.00	20.42	70.50	29.11	62.50	31.14	60.50	30.31	60.50
	PAD	<b>90.07</b>	<b>21.67</b>	<b>68.50</b>	<b>11.67</b>	<b>79.50</b>	<b>27.22</b>	<b>65.50</b>	<b>31.01</b>	<b>62.00</b>	<b>29.44</b>	<b>61.50</b>
IMDB	Base	93.90	28.89	63.00	16.20	75.00	84.92	13.50	93.55	6.00	28.28	66.00
	ADV	92.07	28.26	62.10	15.83	76.00	58.75	35.20	78.65	21.30	27.20	66.30
	ASCC	92.83	26.11	65.40	13.92	77.50	55.36	38.50	75.37	24.70	25.03	67.00
	DNE	93.05	27.93	63.60	15.83	75.50	53.27	36.50	76.54	25.20	27.05	66.10
	SHIELD	93.88	23.42	69.50	10.73	80.00	56.23	38.50	63.73	32.60	24.87	67.20
	PAD	<b>93.90</b>	<b>20.75</b>	<b>73.00</b>	<b>5.56</b>	<b>85.00</b>	<b>33.33</b>	<b>60.00</b>	<b>54.44</b>	<b>41.00</b>	<b>23.33</b>	<b>68.50</b>
SNLI	Base	86.34	30.30	63.10	38.62	53.40	61.61	33.40	78.85	18.40	35.27	59.20
	ADV	85.75	31.32	62.40	36.88	56.70	49.73	38.90	75.19	21.00	35.30	58.60
	ASCC	85.33	29.37	64.00	35.83	57.80	48.52	38.60	70.36	27.30	34.29	60.20
	DNE	85.59	29.29	64.20	36.27	58.70	49.01	39.80	72.84	25.10	35.10	62.20
	SHIELD	86.34	27.29	66.70	18.74	76.50	50.41	40.70	68.18	28.20	32.24	62.10
	PAD	<b>86.34</b>	<b>25.02</b>	<b>68.50</b>	<b>5.99</b>	<b>81.60</b>	<b>40.32</b>	<b>51.80</b>	<b>55.53</b>	<b>38.60</b>	<b>28.39</b>	<b>66.30</b>

Table 2: Robustness evaluation results of RoBERTa-based target models.

Method	Character			Word		Sentence
	Acc	VP Rob	DW Rob	TF Rob	BA Rob	SC Rob
Base	89.97	52.50	61.80	33.00	26.40	53.10
ADV <sub>c</sub>	89.78	53.50	68.00	41.50	30.50	49.50
ADV <sub>w</sub>	89.78	51.00	59.20	42.60	31.80	51.00
ADV <sub>s</sub>	89.69	52.00	59.00	30.00	29.50	56.00
ADV <sub>a</sub>	89.69	53.00	67.00	42.50	33.50	54.00
PAD	89.97	55.50	83.50	72.50	73.00	57.50

Table 3: Robustness of MR-BERT with various adversarial training strategies.

than the ADV trained with the specific level of attack. For example, ADV<sub>a</sub> achieves 67.00% Rob under DW while ADV<sub>c</sub> achieves 68.00%. It indicates that there may exist conflicts among the fitting of different levels of attacks for ADV.

**Number of Sub-models** In order to explore the effect of more sub-models for ensemble, we also conduct experiments with five sub-models. The ensemble method improves Rob with an average value of 2%, implying the phenomenon of diminishing marginal returns. As DNNs are no longer weak classifiers, it is difficult to further improve the generalization to some examples out of the distribution.

**Perturb Different Attention Layers** Transformer-based models always contain multiple self-attention layers. Base versions utilized in this paper have  $N = 12$  layers. Some researches observe that BERT (Jawahar et al., 2019) captures surface features at the bottom layer, syntactic features in the middle and semantic features at the top, following the classical tree-like learning structures.

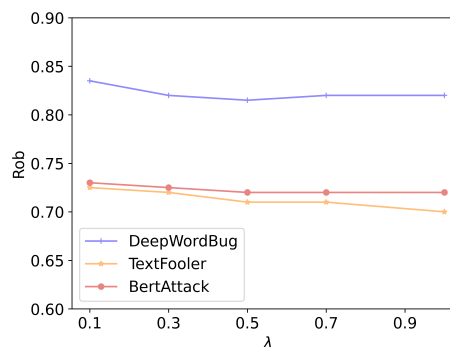


Figure 5: The robustness while performing perturbation with different values of  $\lambda$  of MR-BERT.

We explore the difference in perturbing attention of different layers. Fig. 4 shows the robustness of enhanced MR-BERT for several attacks (DeepWordBug, TextFooler and BertAttack). PAD presents consistent robustness performance on different layers:  $85.50\% \pm 1.41\%$  under DeepWordBug,  $73.78\% \pm 1.09\%$  under TextFooler and  $72.00\% \pm 0.59\%$  under BertAttack.

**Weight of Attention Diversity** We observe the effect while setting the weight of attention diversity  $\lambda$  with different values in  $\{0.1, 0.3, 0.5, 0.7, 1\}$ . Experiment results of MR-BERT are shown in Fig. 5. We find that the Rob decreases when the  $\lambda$  is too large which can not balance the effect of attention diversity in training process.  $\lambda = 0.1$  achieves the best performances for most attacks.

## 5.2. Attention Diversity Visualization

We use *BertViz* (Vig, 2019) to observe the attention matrix. Fig. 6 provides a birds-eye view of attention across all of the sub-models first layer and heads for a randomly sampled input (“*I like this movie, it is really nice!*”). Its rows represent models and columns represent heads. *BertViz* visualizes attention as lines connecting the word being updated (left) with the word being attended to (right) and color intensity reflects the attention weight (darker one means more attention paid).

Sub-models ( $f^1, f^2, f^3$ ) learned by PAD can keep the general attention patterns similar to that of  $f$  with partial changes. The bottom of Fig. 6 shows the attention of head 6.  $f^1, f^2$  and  $f^3$  present diverse attention patterns. The phenomenon is consistent with the learning goal expressed in Eq. 3.2: clean accuracy is kept via maintaining broadly similar attention patterns compared with the base model and minor attention changes diversify the adversarial example distribution of sub-models.

## 6. Related Work

The ensemble method is originally designed to improve generalization performance (Kuncheva and Whitaker, 2003; Wen et al., 2020; Sinha et al., 2021), which can boost multiple weak classifiers to a strong classifier. With the growing interest of the deep learning community in robustness issues, the possibility of improving the robustness of the model with an ensemble method was recently explored. For image, Pang et al. (2019) try to achieve the ensemble’s robustness improvement via promoting the diversity among non-maximal predictions of individual members.

However, the work of He et al. (2017) implies that ensemble of weak defenses is not sufficient to provide a strong defense against adversarial examples. In recent, Yang et al. (2022c) try to establish the relationship between ensemble and gradient diversity for image classifiers based on the model smoothness assumption. For NLP, ensemble method for robustness improvement is still under-explored especially due to that NLP models face various types of attacks. In 2022, Le et al. (2022) modifies and re-trains the last layer of a well-trained NN and utilizes a stochastic weighted ensemble of sub-models for prediction. Since the parameters of the feature extraction module are frozen, this method may not be able to eliminate the presence of adversarial samples in the feature extraction step. Our method utilizes the attention diversity to realize a robust ensemble. It can diversify the sub-models with good interpretability.

## 7. Conclusion

In this paper, we propose an ensemble method PAD which utilizes attention diversity to enhance robustness against different attacks. Compared to previous efforts that focus on enhancing defense ability against a specific type of attack, we provide a novel approach to improve general defense. In order to save memory and computation resources, PAD applies a scheme of adding plugins to the self-attention layer which can dynamically generate multiple sub-models for training and inference. Experiments on three NLP tasks and two target models show that PAD significantly improves robustness under three levels of attacks including five attack methods.

## Limitations

The approach to promoting attention diversity in this paper is only applicable to Transformer-based neural networks. For other neural networks like CNNs and LSTMs, our plugin is also applicable, however, it may not be interpretable like attention. Besides, since our ensemble method does not introduce data outside the training set, the sub-models may not be able to generalize well to out-of-distribution adversarial samples.

## Ethics Statement

With the emergence of more and more adversarial scenarios, few perturbations, e.g., modifying some words with their synonyms, can mislead a well-trained DNN’s prediction. It arises society’s concern about the safety and applicability of DNNs in piratical scenarios. PAD has an important significance and role in building a trustworthy AI system. The general defense ability under different levels of attacks indicates that general defense for different adversarial scenarios is promising. The visualization of attention can also assist the society in understanding the inner mechanism of the ensemble. Our work does not arise ethical issues directly and all used datasets are publicly available with no privacy violation.

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Moustafa Alzantot, Yash Sharma, Ahmed Elgohary, Bo-Jhang Ho, Mani B. Srivastava, and Kai-Wei



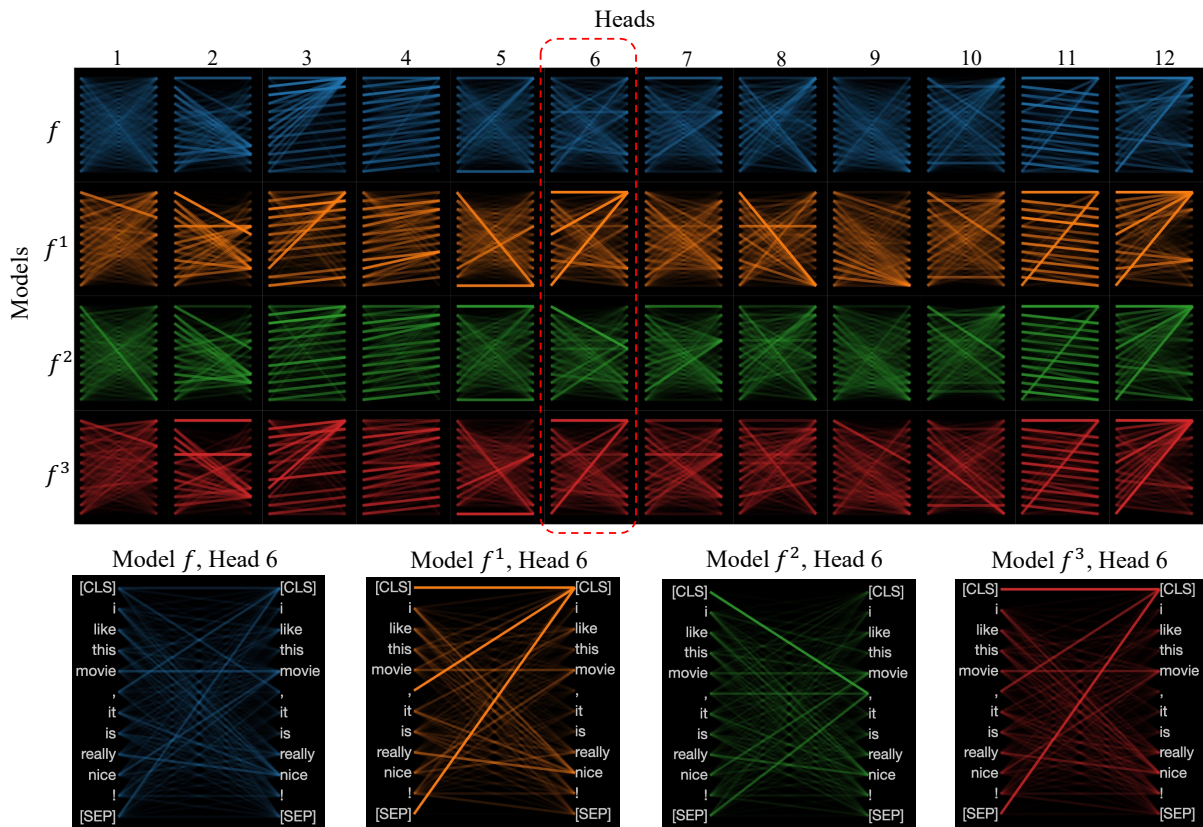


Figure 6: Visualization of attention. Sub-models ( $f^1$ ,  $f^2$ ,  $f^3$ ) in ensemble and the base model ( $f$ ) present different attention patterns.

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