

“CitySense”: Introduction to Probabilistic Modeling

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The CitySense Problem

- Startup company incorporated around 2006.
- Objective: Develop and leverage expertise in **location data** analytics.
- First product was called CitySense¹ (2008).
 - A real-time, data-driven guide to nightlife in San Francisco.

¹See “CitySense: Multiscale space time clustering of GPS points and trajectories” by Markus Loecher and Tony Jebara (2009). <http://www.cs.columbia.edu/~jebara/papers/CitySense.JSM2009.pdf>

CitySense (2008)

The screenshot shows the CitySense app interface on an iPhone. At the top, it says "Citysense™ Live San Francisco Nightlife Activity". Below this is the question "Where is everybody?" followed by a bulleted list of features: "How busy is the city? Know when to go out", "See the top nightlife hotspots in real-time", "Find out what's there in one click", and "Find out where everyone's going next" with a "More info" link. There are two app store icons: one for the iPhone App Store and one for the BlackBerry App World. The main part of the screen is a map of San Francisco with a heatmap overlay showing activity levels. A callout box for "Grave St & Hyde St" indicates it was "previously very busy" but is "relatively normal" now. The bottom of the screen shows a navigation bar with a "Normal" button and other icons.

Citysense™
Live San Francisco Nightlife Activity

Where is everybody?

- How busy is the city? Know when to go out
- See the top nightlife hotspots in real-time
- Find out what's there in one click
- Find out where everyone's going next [More info](#)

Citysense
For real-time nightlife on your iPhone®, visit the [App Store](#)

Also available for the BlackBerry®
Go to www.citysense.com on your BlackBerry® to download.

(Sadly, no longer in the App Store.)

Two use cases:

- ① I'm new to the city – where does everybody hang out at night?
- ② I know the city, but is there anything **special** going on tonight?

- Taxi GPS data for sale in San Francisco

The screenshot shows the Yellow Cab Cooperative website. At the top is a dark navigation bar with the Yellow Cab logo and a menu: HOME (highlighted), SERVICE, FAQs, ACCOUNTS, ABOUT, CONTACT, and SAN FRANCISCO. Below the navigation bar, the date "TUESDAY, MAY 01, 2012" and a "TEXT SIZE" control are visible. On the left is a sidebar menu with links: Home, Service, FAQs, Accounts, About, Contact, and San Francisco. The main content area features a large advertisement for Yellow Cabs with the headline "YELLOW MAKES IT EASY." and text: "The second time you call from your home or work phone our auto dispatch system recognizes your address. You have the option to request service by using one button on your phone without speaking to a service call taker." Below the ad is a yellow taxi. At the bottom, there are sections for "Our History" and "Our Community".

- Main Idea: Taxi destinations are a proxy for where people are going.
- Can use taxi data to bootstrap
 - Once we had users, we could use the locations from their phones.
- Taxi feed is **real-time**, so can use it to find those big secret parties.

Data Science Strategy

- ① Model “typical” behavior of each area of the city.
- ② Rank areas with activity levels that are “most unusual”.

We'll discuss modeling strategies shortly.

Plan for this lecture

- Examine the CitySense “anomaly detection” problem.
- But use the NYC taxi pickup data – more local and more recent.
- Our dataset is from 2009.
- Currently (2017/11/09) you can download 2013 data from <https://github.com/andresmh/nyctaxitrips>
- You can also request data directly from the NYC Taxi and Limousine Commission via the Freedom of Information Law.
<http://www.nyc.gov/html/tlc/html/passenger/records.shtml>

The Case for Probability Models

Predicting Probability Distributions

So far we've discuss two problem classes:

- **Classification**

- Outcome space $\mathcal{Y} = \{-1, 1\}$
- Action space $\mathcal{A} = \mathbf{R}$ (threshold to get hard classifications)

- **Regression**

- Outcome space $\mathcal{Y} = \mathbf{R}$
- Action space $\mathcal{A} = \mathbf{R}$.

- Today we consider a third type of **action space**:

$$\mathcal{A} = \{\text{Probability distributions on outcome space } \mathcal{Y}\}$$

- Why?

The Joy of Probability Distributions

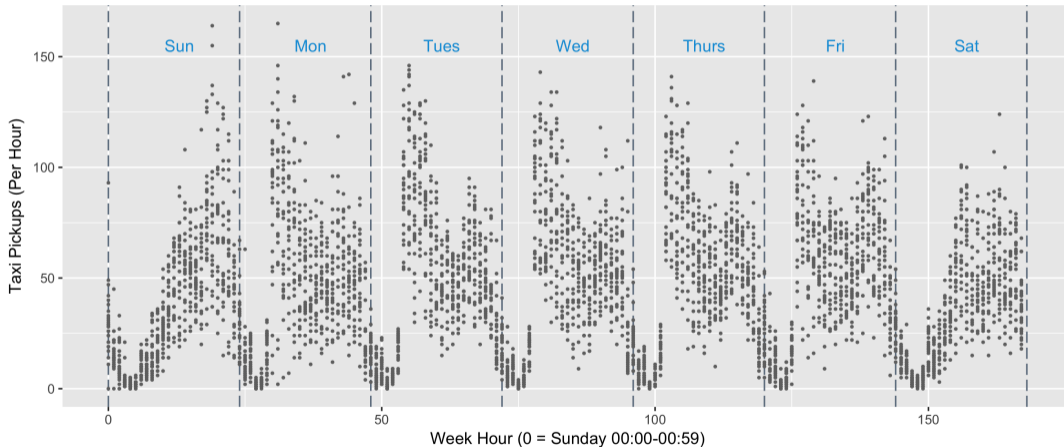
- Outcome space $\mathcal{Y} = \mathbf{R}$ (some regression problem)
- For input x , suppose we produce a **probability density** on \mathcal{Y} :

$$x \mapsto p(y)$$

- We can interpret this setting as modeling the **conditional probability density** $p(y | x)$.
- If we know $p(y | x)$, we can find a \hat{y} that minimizes any loss function for a given x :
 - For square loss, give the mean of $p(y | x)$. [From homework]
 - For ℓ_1 loss, give the median of $p(y | x)$. [From homework]
 - Can produce a **prediction interval** that $p(y | x)$ assigns a 95% probability
-

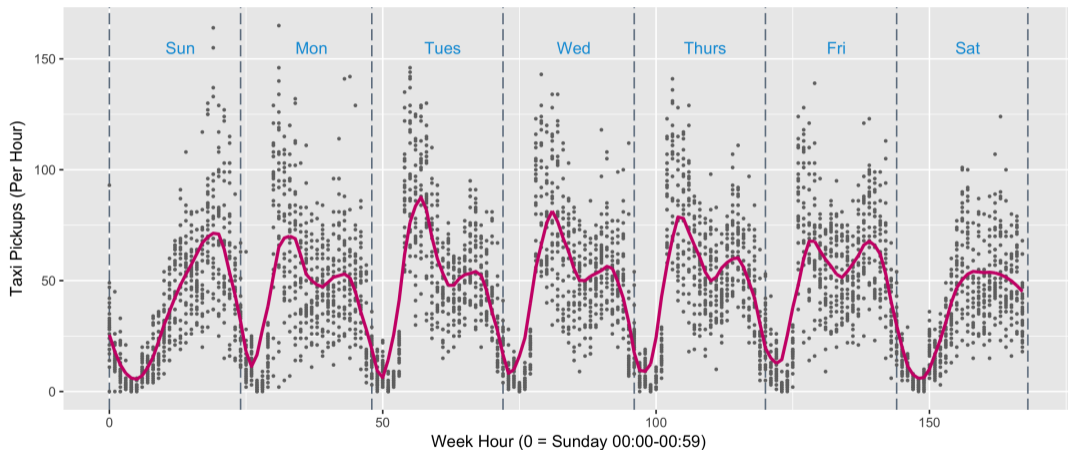
Penn Station Taxi Pickup Counts - 27 Weeks

Penn Station Taxi Pickups, by Hour-of-Week (27 Weeks)



Penn Station Taxi Pickup Counts - Regression

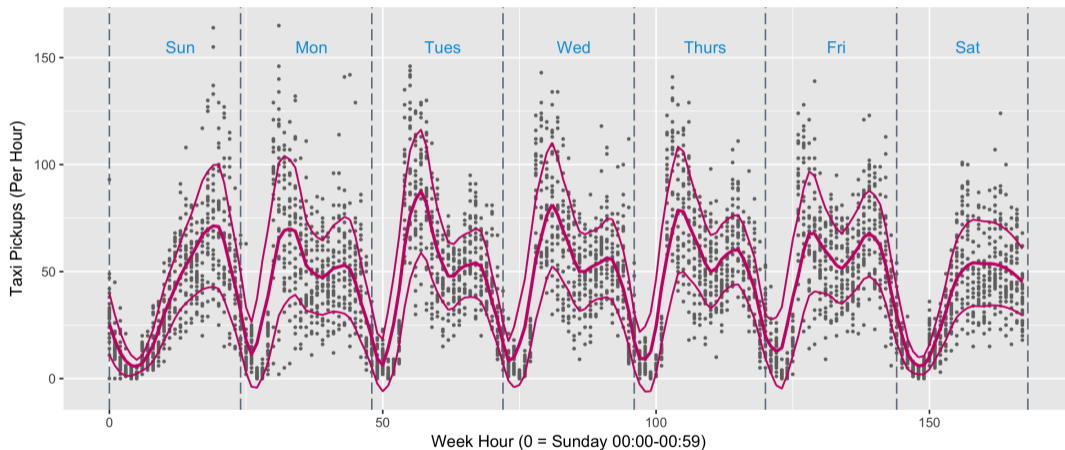
Penn Station Taxi Pickups, by Hour-of-Week (27 Weeks)



Regression line predicts **mean pickups**. But what's the typical range?

Penn Station Taxi Pickup Counts - Prediction Intervals

Penn Station Taxi Pickups, by Hour-of-Week (27 Weeks)



Here plotting estimated ± 1 standard deviation.

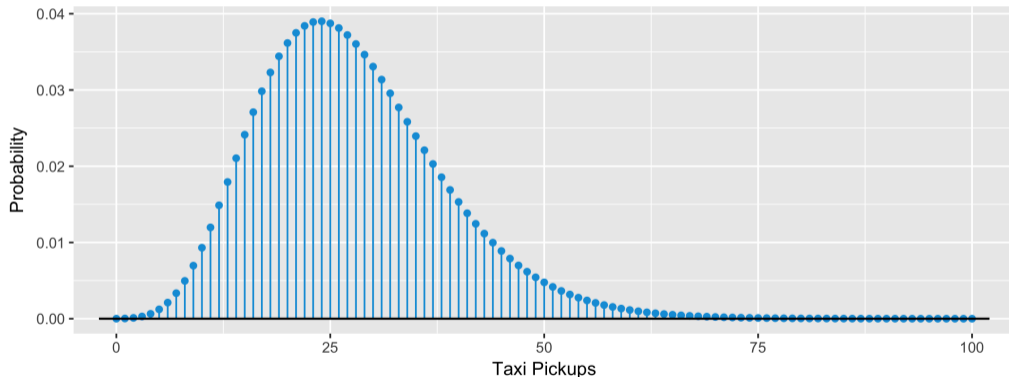
Penn Station Taxi Pickup Counts - Predictive Distribution

- Consider predictions for a particular weekhour $x \in \{0, \dots, 167\}$, say $x = 10$.
- **Regression** gives a single number: $\mathbb{E}[y \mid x = 10] \approx \mathbf{30.1}$ taxi pickups
- A **prediction interval** gives two numbers: $\mathbb{P}(y \in [\mathbf{17.8}, \mathbf{42.3}] \mid x = 10) \approx 68\%$.
- We can also produce an estimate of the full **conditional probability distribution** for $p(y \mid x = 10)$...

Penn Station Taxi Pickup Counts - Predictive Distribution

- For weekhour 10 (i.e. $x = 10$), we predict the following distribution for $p(y | x = 10)$:

Predicted Distribution for Pickup Count (Penn Station, Week Hour = 10)



- According to this predictive distribution, how likely are we to get 90 taxi pickups?

Predictive Distributions for Anomaly Characterization

- At week-hour 10,
 - the expected number of taxi pickups 30.1.
 - the 68% prediction interval was [17.8, 42.3].
- Suppose we observe 90 taxi pickups.
- How can we characterize how unusual this event is?
- We can directly calculate the probability of 90 or more taxi pickups:

$$\mathbb{P}(y \geq 90 \mid x = 10) = \sum_{c=90}^{\infty} p(y = c \mid x = 10)$$

measures how unusual this event is.

Prediction Intervals from Probability Distributions

- Given a conditional probability distribution $p(y | x)$,
 - it's usually straightforward to compute a **prediction interval**.
- A 95% prediction interval is an interval $[a, b]$ such that

$$\mathbb{P}(y \in [a, b] | x) \approx .95$$

- We can get $[a, b]$ by finding the 2.5% and 97.5% quantiles of the distribution $p(y | x)$.
- [Alternatively, can do this with **quantile regression**.]

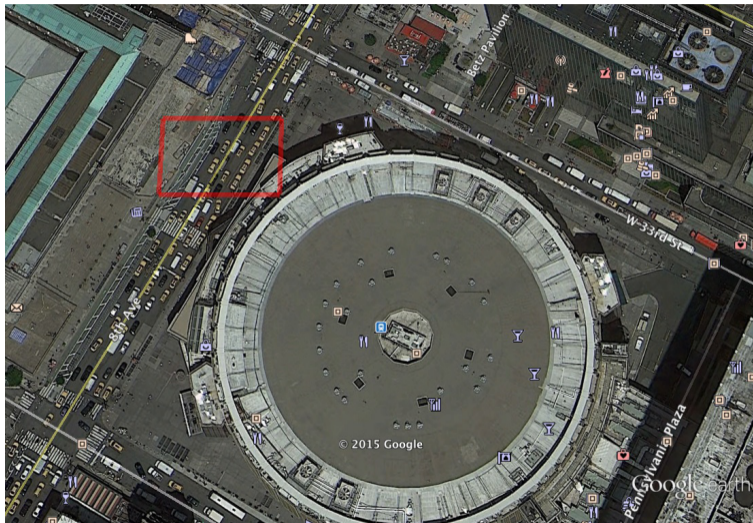
The Grid Cells

The Basic Approach

- Raw input is [roughly] continuous in
 - space (lat/lon) and
 - time (seconds since 1970-01-01).
- To make it easier to handle, we partition space and time into buckets.
- Spatial partitioning
 - Divide earth into regularly spaced grid cells.
 - About 400,000 grid cells to cover NYC
- Time partitioning
 - Only consider times at the hour level.
- Aggregate taxi pickup counts at the Grid Cell / Hour level.

Initial data analysis, including aggregation by grid cell and hour, was done by Blake Shaw.

Most Active Grid Cell: Penn Station (Grid ID 7750)

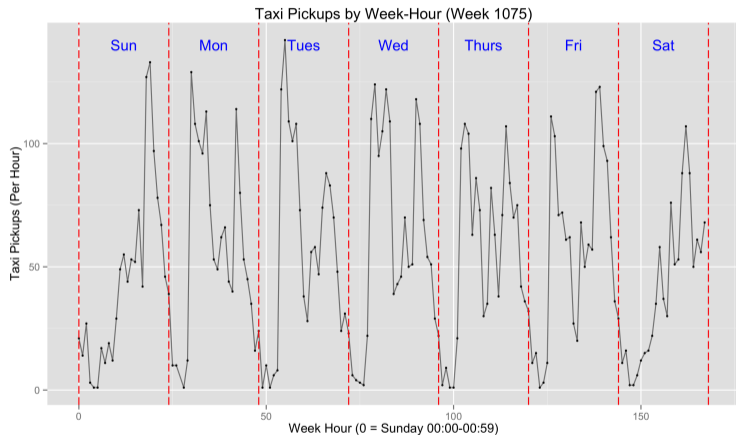


Courant Institute (Grid ID 21272)



Data Visualization

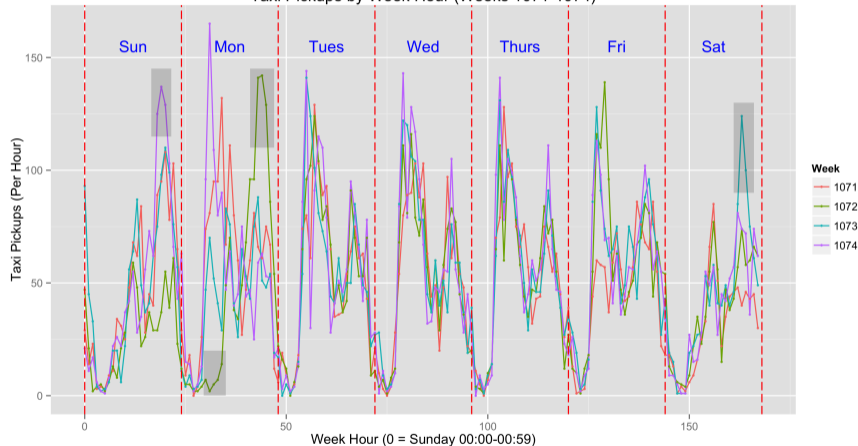
Penn Station (Cell 7750): 1300 Taxi Pickups Per Day



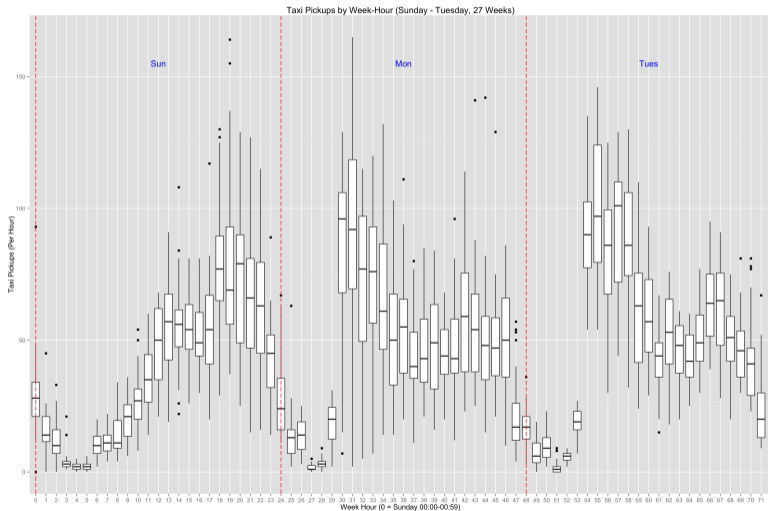
Note difference between weekend and weekday patterns.

Penn Station (Cell 7750): Four Weeks, Some Outliers

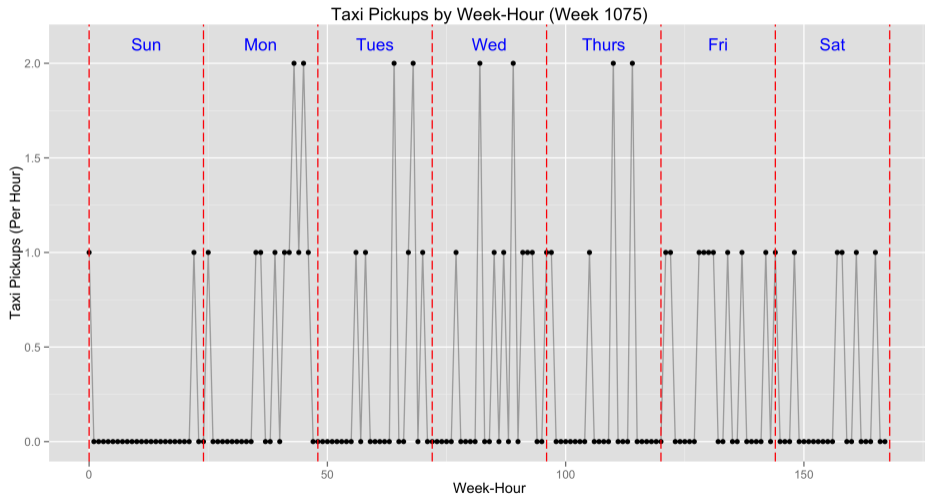
Taxi Pickups by Week Hour (Weeks 1071-1074)



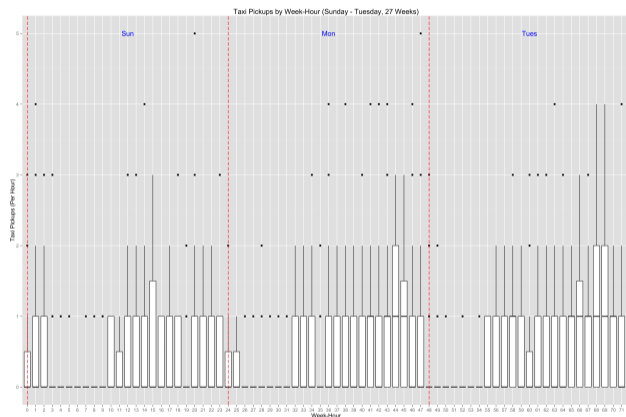
Penn Station: Sunday-Tuesday, 27 Weeks



Courant (Week 1075): 12 Taxi Pickups Per Day



Courant Institute: Sunday-Tuesday, 27 Weeks



Note: At least 25%, sometimes 75%+ of counts are zero. Box plot clearly shows extreme values (ranging up to 5).

The Prediction Problem

The Prediction Problem

Somebody queries a **grid cell** and a **week-hour**, we tell them what to expect.

- Input space: $\mathcal{X} = \{(g, h) \mid g \in \{1, \dots, 398245\} \text{ and } h \in \{0, \dots, 167\}\}$, where
 - g is the grid Cell ID and
 - h is the week-hour
 - Possible future inputs: Holiday? Raining? Special event?
- Action space: $\mathcal{A} = \{\text{Probability distributions on number of pickups}\}$
- Outcome space: $\mathcal{Y} = \{0, 1, 2, 3, \dots\}$
 - Actual number of taxi pickups.
- Evaluation? Loss function? We'll come back to these questions...

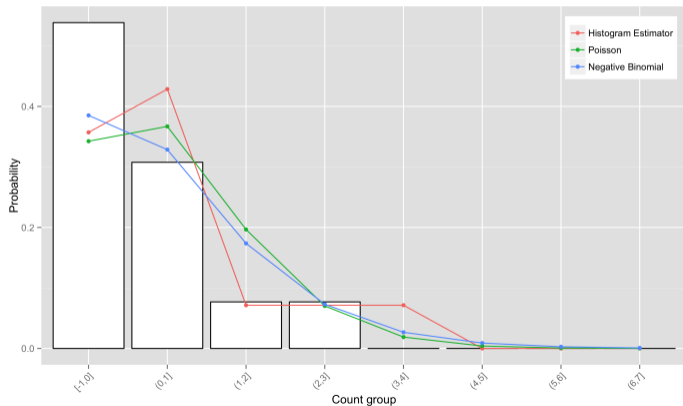
Setting up the Learning Problem

- Labeled data look like:
 - (Grid Cell = 10321, Week Hour = 120) \mapsto Count = 3
 - (Grid Cell = 192001, Week Hour = 6) \mapsto Count = 12
 - (Grid Cell = 1271, Week Hour = 154) \mapsto Count = 0
- How to split the data into a training set and a test set?
- Our approach:
 - First 14 weeks are **training set**.
 - Last 13 weeks are **test set**.

Stratification Approaches

Approach 1: Full Stratification (Courant, Tuesdays 7-8pm)

- Estimate distribution for each grid cell / week hour pair.
- Colored lines are from training. White bars are from test.



Terminology: Stratification and Bucketing

Definition

We say we are **stratifying** if we partition our input space into groups, and treat each group separately. For example, in modeling we would build a separate model for each group, without information sharing across groups.

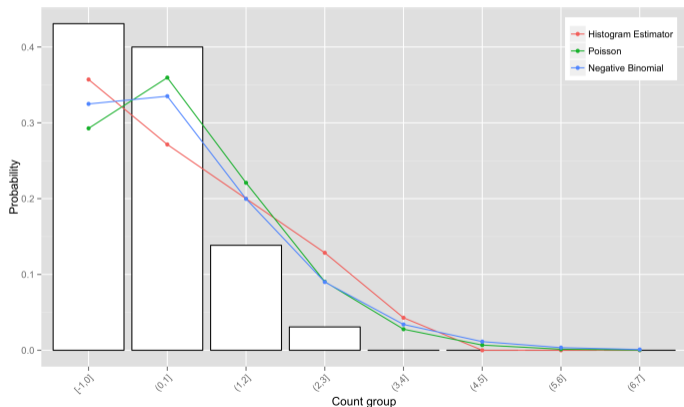
On the other hand,

Definition

We say we are **bucketing** (or **binning**) if we are combining natural groups in the data into a single group, rather than building a separate model for each group. For example, combining all weekdays together would be “bucketing”.

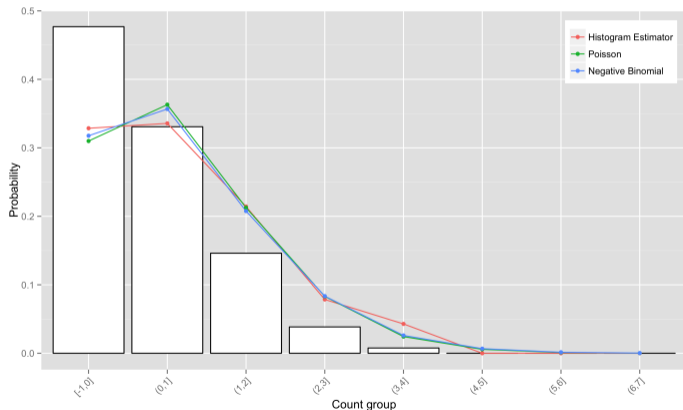
Approach 2: Weekday Bucketing (Courant, M-F 7-8pm)

- Data inspection suggests that day patterns are similar Mon-Fri.



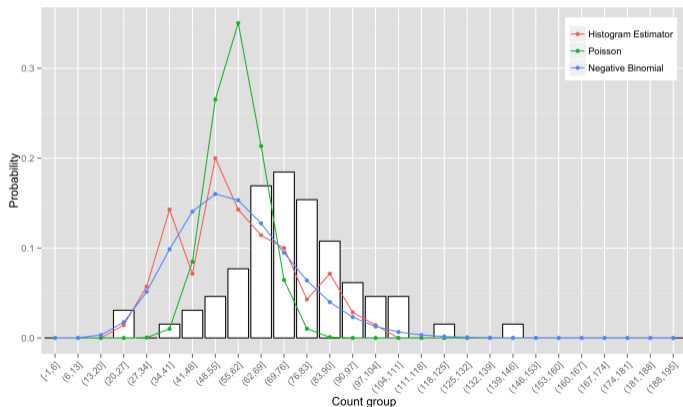
Approach 3: (Courant, M-F 6-8pm)

- Also, 6-7pm looks similar to 7-8pm, so join together



Penn Station, M-F 7-8pm

- Negative binomial fits empirical much better than Poisson. (overdispersion)
- Massive shift between train and test!



The Estimation/Approximation Tradeoff of Stratification

- With a separate probability distribution for every grid cell / week-hour pair, model is highly specific!
- Could capture idiosyncrasy of Friday @5pm that we would miss if combining all weekdays.
 - That is, we're decreasing approximation error.
- With relatively little data in a particular stratum, estimates may have high estimation error.
- By “bucketing”, or combining strata:
 - We can reduce estimation error.
 - It may cost us in approximation error.
 - By bucketing in a smart way, you can minimize increase in approximation error.
- Note: This is often referred to as a **bias / variance tradeoff**:
 - $\text{bias} \approx \text{approximation error}$; $\text{variance} \approx \text{estimation error}$

Is there a more convenient way?

- We can tradeoff between estimation and approximation error by varying the stratification and the bucketing.
- It's a great way to start your data analysis.
 - You get a feel for the data and gain some intuition.
- Our classification and regression techniques also trade off between approximation and estimation:
 - We had to choose our features.
 - We had to tune our regularization parameter.
- Can we do something similar for predicting distributions?
- Yes – to be discussed in our module on conditional probability modeling.